**Western Australian Certificate of Education**

**Semester One Examination, 2020**

**Question/Answer Booklet**

**MATHEMATICS**

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98

**SPECIALIST**

**UNIT 1&2**

**Section Two:**

**Calculator- assumed Score for this booklet**

**Student’s Name**: **\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**As shown on your exam timetable.**

**Student’s Teacher Mr Bradbury Mrs Waddell**

(**Circle your teacher’s name**.)

**Time allowed for this section**

Reading time before commencing work: ten minutes

Working time for this section: one hundred minutes

**Materials required/recommended for this section**

***To be provided by the supervisor***

This question /Answer Booklet

Formula Sheet (retained from Section One)

***To be provided by the candidate***

Standard Items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters.

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

and up to three calculators approved for use in the WACE examinations.

**Important note to candidates**

No other items may be taken into the examination room. It is **your** responsibility to ensure

that you do not have any unauthorized notes or other items of a non-personal nature in the

examination room. If you have any unauthorized material with you, hand it to the supervisor

**before** reading any further.

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| --- | --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | | Working time (minutes) | Marks available | Percentage of exam |
| Section One:  Calculator-free | 8 | 8 | | 50 | 52 | 35 |
| Section Two:  Calculator-assumed | 13 | 13 | | 100 | 98 | 65 |
|  | | | **Total** | | 150 | 100 |

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the *School Examination Rules* provided with your exam timetable.Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet preferably using a blue/black pen.

Do not use erasable or gel pens.

1. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
2. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

* Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
* Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

1. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
2. It is recommended that you **do not use pencil**, except in diagrams.
3. The formula sheet and your notes are **not to be handed** in with your Question/Answer Booklet.

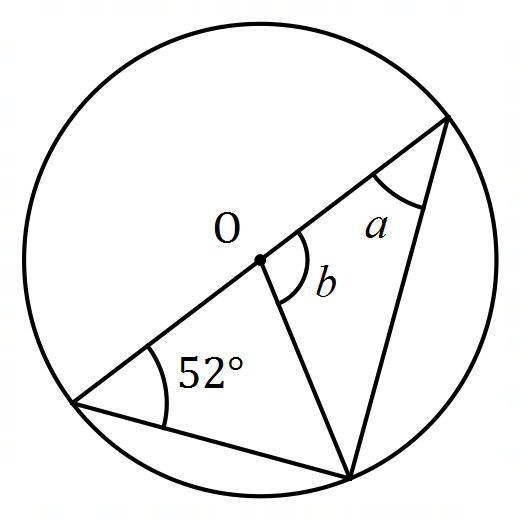
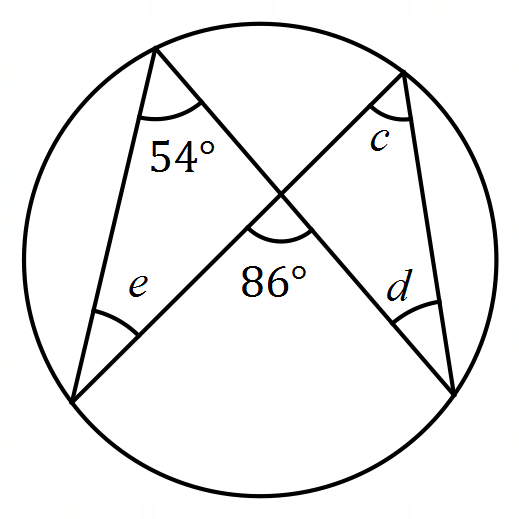
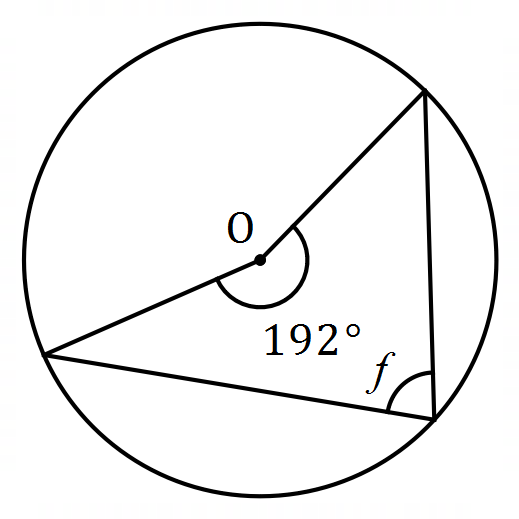
Section Two: Calculator-assumed 65% (98 Marks)

This section has**thirteen** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 (6 marks)

Determine the size of the angles marked and shown in the circles below. Where marked, is the centre of the circle.

Question 10 (5 marks)

Three forces act on an object so that it remains in equilibrium. Two of the forces have magnitudes of N and N and the angle between their directions is . Determine the magnitude of the third force and the angle its direction makes with the smaller force.

Question 11 (8 marks)

(a) An art gallery plans to display a single painting on each of the three walls in a room. Determine how many arrangements of paintings are possible in the room if they have a selection of different paintings to choose from. (2 marks)

(b) In another room, the gallery plan to hang different paintings in a row. If of the paintings are by the artist Marr, determine the number of different arrangements of paintings that are possible when

(i) the paintings by Marr must be at the ends. (2 marks)

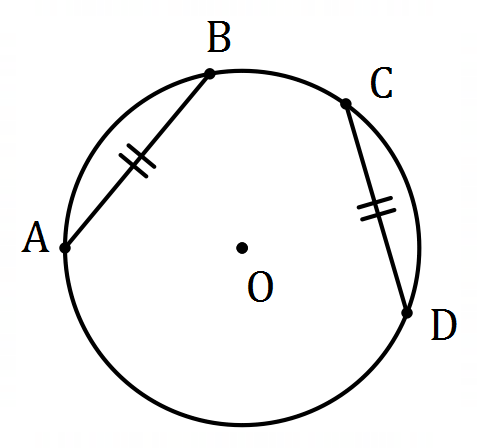
(ii) the paintings by Marr must be next to each other. (2 marks)

(iii) the paintings by Marr must be apart and not at the ends. (2 marks)

Question 12 (8 marks)

(a) Prove that chords of equal length subtend equal angles at the centre of a circle.

(3 marks)

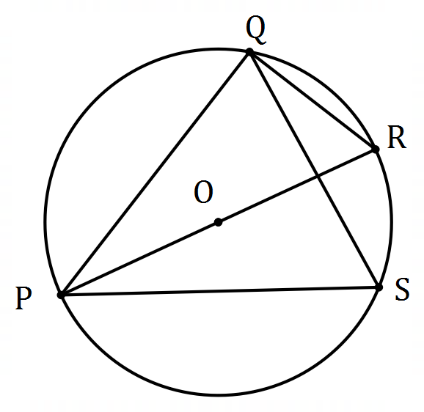


(b) Points and lie on a circle of radius cm so that cm. Determine

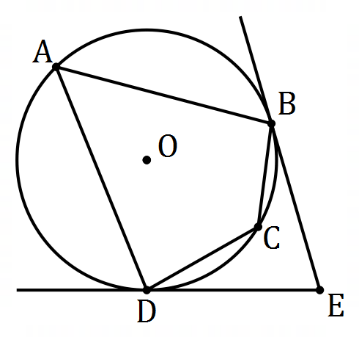
(i) the distance of chord from the centre of the circle. (3 marks)

(ii) the angle subtended by chord at the centre of the circle. (2 marks)

Question 13 (7 marks)

(a) The diagram shows points and that  
lie on the circumference of a circle centre .  
 is a diameter and the size of .

Determine, with reasons, the size of . (3 marks)



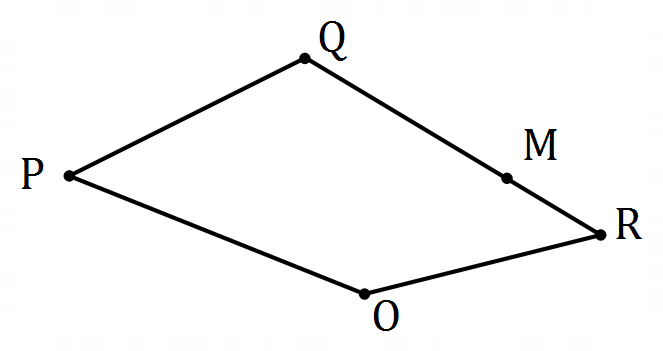
(b) In the diagram shown, and are points  
on the circumference of a circle with centre .

Tangents to the circle at and intersect at .

Determine, with justification, the size of   
when . (4 marks)

Question 14 (8 marks)

In quadrilateral shown below, lies on so that .



(a) If and , express the following in terms of and/or .

(i) . (1 mark)

(ii) . (2 marks)

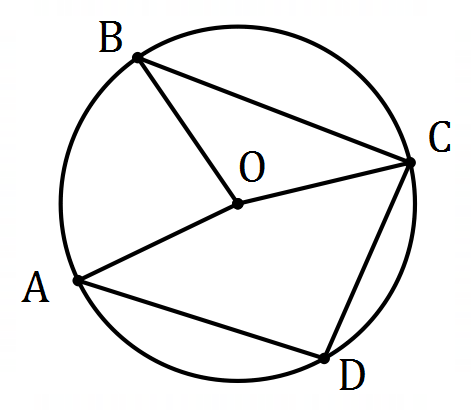
(iii) . (2 marks)

(b) If is the origin and points and have coordinates and respectively, determine the distance . (3 marks)

Question 15 (8 marks)

(a) The vertices of quadrilateral lie on the circumference of a circle centre shown below. Given that and , determine with reasoning the size of angle .

(4 marks)



(b) The vertices of triangle lie on the circumference of a circle. Given that cm,

cm and cm, prove by contradiction that is not a diameter of the circle.

(4 marks)

Question 16 (7 marks)

(a) A calculator can generate random integers between and . Use the pigeonhole principle to explain why random integers should be generated to be certain that at least of them are the same. (3 marks)

(b) customers bought a total of items from a supermarket. Given that each customer bought at least one item, show that at least two of the customers bought the same number of items. (4 marks)

Question 17 (9 marks)

(a) Determine the scalar product of

(i) and . (1 mark)

(ii) two vectors with directions apart that have magnitudes of and . (1 mark)

(b) Given that and simplify . (3 marks)

(c) The position vectors of points and are and . Show use of a vector method to determine the size of angle . (4 marks)

Question 18 (8 marks)

A school yearbook is produced by a committee of teachers and students. teachers and students have nominated for the committee.

(a) Determine how many different committees could be formed from the nominations.

(2 marks)

(b) The student nominations include two sets of twins. Determine how many different committees could be chosen that include at least one set of twins. (4 marks)

(c) Suppose one of the teachers in the committee will be appointed as treasurer and one of the students will be appointed as secretary. Determine how many different committees can be formed with this structure. (2 marks)

Question 19 (8 marks)

Oil platform T lies km away from another oil platform F on a bearing of . A steady current of km per hour flows between the platforms on a bearing of . A small boat at F, with a cruising speed of km per hour, needs to arrive at T by pm.

Determine the bearing that the boat should steer and the latest time it should depart from F.

Question 20 (8 marks)

Circles and intersect at points and . passes through , the centre of . lies on so that line segment is tangential to at . Let .

(a) Sketch a diagram to show the above information. (3 marks)

(b) Determine in terms of . (1 mark)

(c) Explain why . (1 mark)

(d) Prove that . (3 marks)

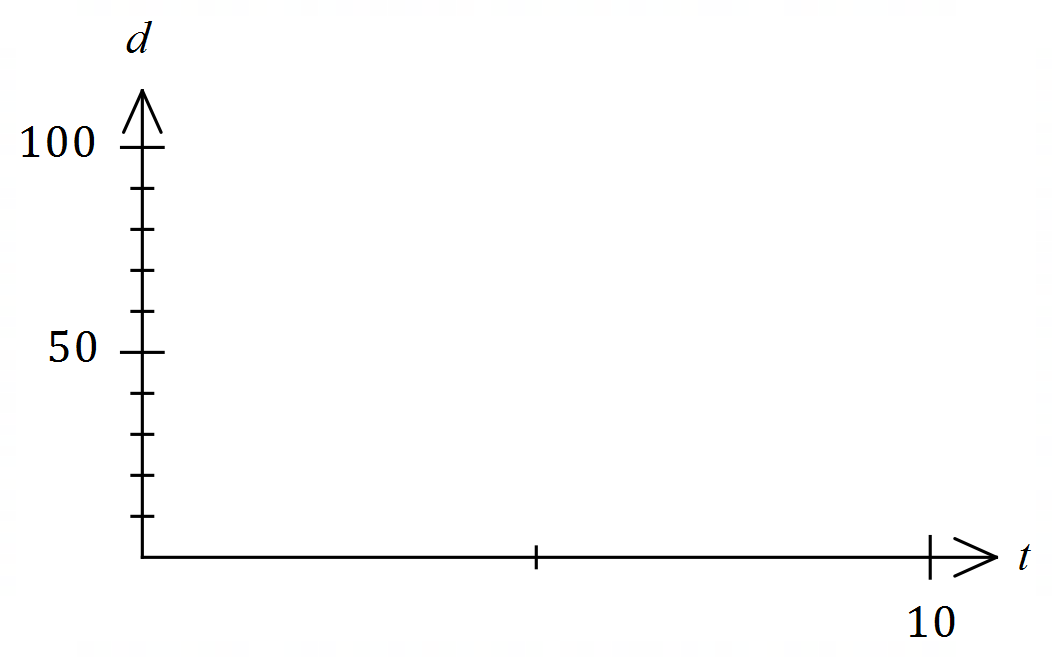
Question 21 (8 marks)

Particle , initially at the point with position vector cm, moves with a constant velocity of cm/s. Particle is stationary at the point with position vector .

(a) Determine the initial distance of from . (2 marks)

(b) Determine an expression for the distance between and after seconds. (3 marks)

(c) Sketch a graph of against and hence determine the time that minimises and state what this minimum distance is. (3 marks)



**Additional working space.**

**Question Number:\_\_\_\_\_\_\_\_\_**

**Additional working space.**

**Question Number: \_\_\_\_\_\_\_\_\_**

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